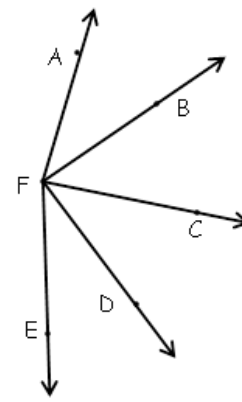


Level 1: A

Given:  $\angle AFB \cong \angle DFE$

Prove:  $m\angle CFD + m\angle AFB = m\angle CFE$



Statement

Reason

1.  $\angle AFB \cong \angle DFE$  or  $m\angle AFB = m\angle DFE$

1. Given

2.  $m\angle CFD + m\angle DFE = m\angle CFE$

2. Angle Addition Postulate

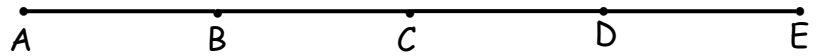
3.  $m\angle CFD + m\angle AFB = m\angle CFE$

3. Substitution Property

Level 1: B

Given:  $\overline{AB} \cong \overline{DE}$

Prove:  $\overline{CD} + \overline{AB} = \overline{CE}$



Statement

Reason

1.  $\overline{AB} \cong \overline{DE}$  or  $AB = DE$

1. Given

2.  $CD + DE = CE$

2. Segment Addition Postulate

3.  $CD + AB = CE$

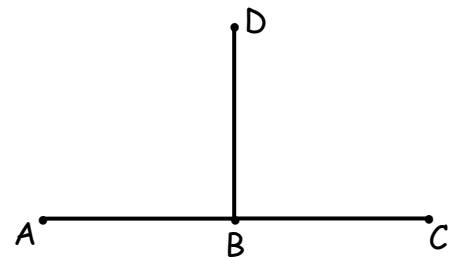
3. Substitution Property

Level 1: C

Given: B is the midpoint of  $\overline{AC}$ ;

$AB = BD$

Prove:  $BD = BC$



Statement

Reason

1. B is the midpoint of  $\overline{AC}$

1. Given

2.  $AB = BC$

2. Definition of Midpoint

3.  $AB = BD$

3. Given

4.  $BD = BC$

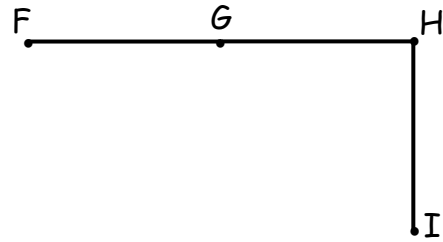
4. Substitution Property

Level 1: D

Given:  $G$  is the midpoint of  $\overline{FH}$ ;

$$\overline{FG} \cong \overline{HI}$$

Prove:  $\overline{GH} \cong \overline{HI}$



**Statement**

1.  $G$  is the midpoint of  $\overline{FH}$
2.  $\overline{FG} \cong \overline{GH}$
3.  $\overline{HI} \cong \overline{GH}$
4.  $\overline{GH} \cong \overline{HI}$

**Reason**

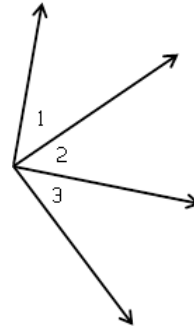
1. Given
2. Definition of Midpoint
3. Substitution Property
4. Symmetric Property

Level 2: A

Given:  $\angle 1$  and  $\angle 2$  are comp.  $\angle$ 's;

$\angle 2$  and  $\angle 3$  are comp.  $\angle$ 's

Prove:  $m\angle 1 = m\angle 3$



**Statement**

1.  $\angle 1$  and  $\angle 2$  are comp.  $\angle$ 's;  
 $\angle 2$  and  $\angle 3$  are comp.  $\angle$ 's
2.  $m\angle 1 + m\angle 2 = 90$   
 $m\angle 2 + m\angle 3 = 90$
3.  $m\angle 1 + m\angle 2 = m\angle 2 + m\angle 3$
4.  $m\angle 1 = m\angle 3$
5.  $m\angle 1 = m\angle 3$

**Reason**

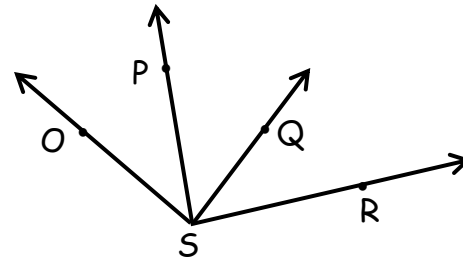
1. Given
2. Def. of Comp.  $\angle$ 's
3. Substitution Property
4. Reflexive Property
5. Subtraction Property

Level 2: B

Given:  $\overline{SP}$  bisects  $\angle OSQ$ ;

$\overline{SQ}$  bisects  $\angle PSR$

Prove:  $\angle OSP \cong \angle QSR$



**Statement**

1.  $\overline{SP}$  bisects  $\angle OSQ$ ;  
 $\overline{SQ}$  bisects  $\angle PSR$

2.  $m\angle OSP = m\angle PSQ$   
 $m\angle PSQ = m\angle QSR$

3.  $m\angle OSP = m\angle QSR$

**Reason**

1. Given

2. Def. of Angle Bisector

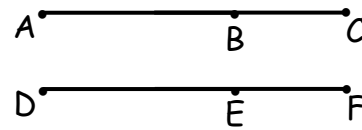
3. Substitution Property

Level 2: C

Given:  $AB = DE$ ;

$BC = EF$

Prove:  $AC = DF$



**Statement**

1.  $AB = DE$ ;  
 $BC = EF$

2.  $AB + BC = DE + EF$

3.  $AB + BC = AC$ ;  
 $DE + EF = DF$

4.  $AC = DF$

**Reason**

1. Given

2. Addition Property

3. Segment Addition Property

4. Substitution Property

Level 2: D

Given:  $MO = NP$

Prove:  $MN = OP$



**Statement**

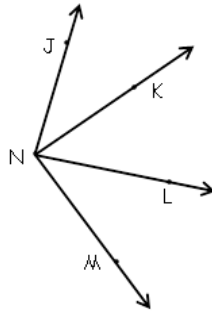
**Reason**

- |                                     |                               |
|-------------------------------------|-------------------------------|
| 1. $MO = NP$ ;                      | 1. Given                      |
| 2. $MN + NO = MO$<br>$NO + OP = NP$ | 2. Segment Addition Postulate |
| 3. $MN + NO = NO + OP$              | 3. Substitution Property      |
| 4. $NO = NO$                        | 4. Reflexive Property         |
| 5. $MN = OP$                        | 5. Subtraction Property       |

Level 3: A

Given:  $\angle JNK \cong \angle LNM$

Prove:  $\angle JNL \cong \angle KNM$



**Statement**

**Reason**

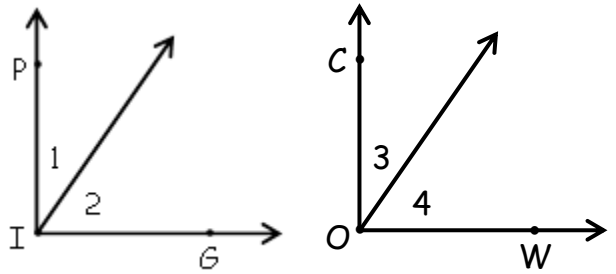
- |   |                             |
|---|-----------------------------|
| 1. $\angle JNK \cong \angle LNM$ or $m\angle JNK = m\angle LNM$ ;                           | 1. Given                    |
| 2. $m\angle KNL = m\angle KNL$  | 2. Reflexive Property       |
| 3. $m\angle JNK + m\angle KNL = m\angle KNL + m\angle LNM$                                  | 3. Addition Property        |
| 4. $m\angle JNK + m\angle KNL = m\angle JNL$ ;<br>$m\angle KNL + m\angle LNM = m\angle KNM$ | 4. Angle Addition Postulate |
| 5. $m\angle JNL = m\angle KNM$ or $\angle JNL \cong \angle KNM$                             | 5. Substitution Property    |

Level 3: B

Given:  $m\angle PIG = m\angle COW$

$m\angle 1 = m\angle 4$

Prove:  $m\angle 2 = m\angle 3$



**Statement**

1.  $m\angle 1 + m\angle 2 = m\angle COW$  ;
2.  $m\angle 1 + m\angle 2 = m\angle PIG$   
 $m\angle 3 + m\angle 4 = m\angle COW$
3.  $m\angle 1 + m\angle 2 = m\angle 3 + m\angle 4$
4.  $m\angle 1 = m\angle 4$
5.  $m\angle 2 = m\angle 3$

**Reason**

1. Given
2. Angle Addition Postulate
3. Substitution Property
4. Given
5. Subtraction Property

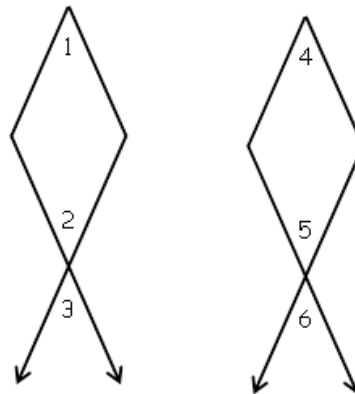
Level 3: C

Given:  $m\angle 1 = m\angle 3$

$m\angle 4 = m\angle 6$

$m\angle 1 = m\angle 4$

Prove:  $m\angle 2 = m\angle 5$



**Statement**

1.  $m\angle 1 = m\angle 3$ ;  $m\angle 4 = m\angle 6$ ;  $m\angle 1 = m\angle 4$
2.  $m\angle 3 = m\angle 4$
3.  $m\angle 3 = m\angle 6$
4.  $m\angle 2 = m\angle 3$ ;  $m\angle 5 = m\angle 6$
5.  $m\angle 2 = m\angle 5$

**Reason**

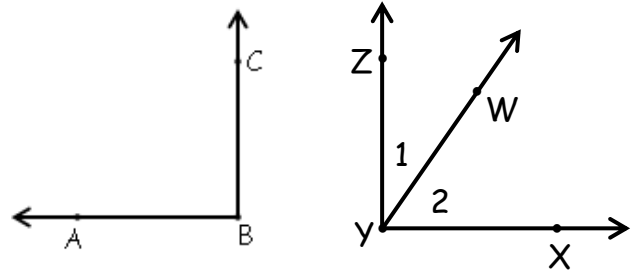
1. Given
2. Substitution Property
3. Substitution Property
4. Vertical Angle Theorem
5. Substitution Property

**Level 3: D**

Given:  $\angle 1$  and  $\angle 2$  are comp.  $\angle$ 's;

$$\overline{AB} \perp \overline{BC}$$

Prove:  $\angle XYZ \cong \angle ABC$



**Statement**

1.  $\angle 1$  and  $\angle 2$  are comp.  $\angle$ 's

2.  $m\angle 1 + m\angle 2 = 90$

3.  $m\angle 1 + m\angle 2 = m\angle XYZ$

4.  $m\angle XYZ = 90$

5.  $\overline{AB} \perp \overline{BC}$

6.  $m\angle ABC = 90$

7.  $m\angle XYZ = m\angle ABC$  or  $\angle XYZ \cong \angle ABC$

**Reason**

1. Given

2. Def. of comp.  $\angle$ 's

3. Angle Addition Postulate

4. Substitution Property

5. Given

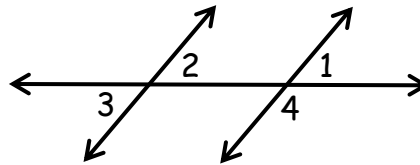
6. Def. of Perpendicular Lines

7. Substitution Property

**Level 4: A**

Given:  $\angle 3$  and  $\angle 4$  are supp.  $\angle$ 's;

Prove:  $\angle 1 \cong \angle 2$



**Statement**

1.  $\angle 3$  and  $\angle 4$  are supp.  $\angle$ 's

2.  $m\angle 3 + m\angle 4 = 180$

3.  $m\angle 1 + m\angle 4 = m\angle 180$

4.  $m\angle 1 + m\angle 4 = m\angle 3 + m\angle 4$

5.  $m\angle 4 = m\angle 4$

6.  $m\angle 1 = m\angle 3$

7.  $m\angle 3 = m\angle 2$

8.  $m\angle 1 = m\angle 2$

**Reason**

1. Given

2. Def. of supp.  $\angle$ 's

3. Angle Addition Postulate

4. Substitution Property

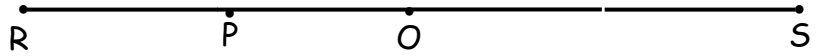
5. Reflexive Property

6. Subtraction Property

7. Vertical Angle Theorem

8. Substitution Property

Level 4: B



Given:  $O$  is the midpoint of  $\overline{RS}$ ;

$P$  is the midpoint of  $\overline{RO}$

Prove:  $RP = \frac{1}{4}RS$

**Statement**

1.  $O$  is the midpoint of  $\overline{RS}$ ;  
 $P$  is the midpoint of  $\overline{RO}$

2.  $RO = \frac{1}{2}RS$ ;  $RP = \frac{1}{2}RO$

3.  $RP = \frac{1}{2}\left(\frac{1}{2}RS\right)$ ;  
 $RP = \frac{1}{4}RS$

**Reason**

1. Given

2. Midpoint Theorem

3. Substitution Property

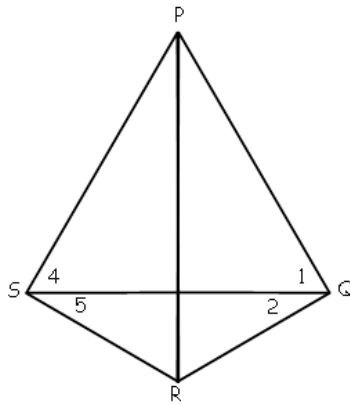
Level 4: C

Given:  $\overline{PQ} \perp \overline{QR}$

$\overline{PS} \perp \overline{SR}$

$\angle 1 \cong \angle 4$

Prove:  $\angle 2 \cong \angle 5$



**Statement**

1.  $\overline{PQ} \perp \overline{QR}$ ;  $\overline{PS} \perp \overline{SR}$

2.  $m\angle PQR = 90$ ;  $m\angle PSR = 90$

3.  $m\angle PQR = m\angle PSR$

4.  $m\angle 1 + m\angle 2 = m\angle PQR$ ;  
 $m\angle 4 + m\angle 5 = m\angle PSR$

5.  $m\angle 1 + m\angle 2 = m\angle 4 + m\angle 5$

6.  $\angle 1 \cong \angle 4$  or  $m\angle 1 = m\angle 4$

7.  $m\angle 2 = m\angle 5$  or  $\angle 2 \cong \angle 5$

**Reason**

1. Given

2. Def. of Perpendicular Lines

3. Substitution Property

4. Angle Addition Postulate

5. Substitution Property

6. Given

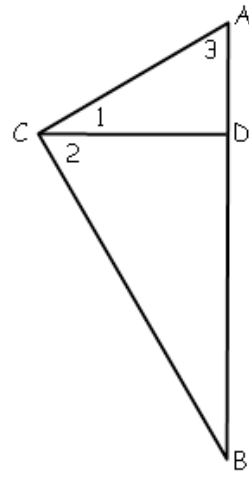
7. Subtraction Property

**Level 4: D**

Given:  $\angle 1$  and  $\angle 3$  are comp.  $\angle$ 's;

$$\overline{AC} \perp \overline{BC}$$

Prove:  $\angle 2 \cong \angle 3$



**Statement**

1.  $\angle 1$  and  $\angle 3$  are comp.  $\angle$ 's

$$2. m\angle 1 + m\angle 3 = 90$$

$$3. \overline{AC} \perp \overline{BC}$$

$$4. m\angle ACB = 90$$

$$5. m\angle 1 + m\angle 2 = m\angle ACB$$

$$6. m\angle 1 + m\angle 2 = 90$$

$$7. m\angle 1 + m\angle 2 = m\angle 1 + m\angle 3$$

$$8. m\angle 1 = m\angle 1$$

$$9. m\angle 2 = m\angle 3$$

**Reason**

1. Given

2. Def. of comp.  $\angle$ 's

3. Given

4. Def. of Perpendicular Lines

5. Angle Addition Postulate

6. Substitution Property

7. Substitution Property

8. Reflexive Property

9. Subtraction Property